

**A statistical study of magnetospheric ion composition along
the geomagnetic field using the Cluster spacecraft for L
values between 5.9 and 9.5**

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Abstract. Using ion density data obtained by the CODIF instrument on-board the Cluster spacecraft, for the interval spanning 2001 - 2005, an empirical model describing the average ion mass distribution along closed geomagnetic field lines is determined. The empirical model describes the region spanning $5.9 \leq L < 9.5$, with dependences on L shell and MLT (Magnetic Local Time) included, and represents ions in the energy range of 0.025 to 40 keV/charge. The data reduction process involves the identification and rejection of CODIF data contaminated by penetrating energetic radiation belt particles, found to frequently occur for $L < 5.9$. Furthermore, a comparison of data with observations of the cold plasma population in the region provides evidence that the CODIF dataset is representative of the full plasma population. The variations in average ion mass along the field lines were modelled using a power law form, which maximises towards the magnetic equatorial plane, with observed power law index values ranging between approximately -2.0 to 0.0. The resulting model illustrates some key features of the average ion mass spatial distribution, such as an average ion mass enhancement at low L in the evening sector, indicating the transport of high latitude heavy ion outflows to the closed inner magnetosphere.

1. Introduction

Variations in magnetospheric plasma mass density provide information on the morphology of the magnetosphere and the different dynamical processes occurring. For example, the magnetospheric mass density plays a crucial role in determining the propagation of wave modes implicated in radiation belt energisation and decay [Meredith *et al.*, 2003; O'Brien *et al.*, 2003]. In addition, the magnetospheric mass density is a significant factor in influencing dayside reconnection rates [Borovsky and Denton, 2006], and therefore has implications for the coupling of the solar wind to the magnetosphere. An important application for models of the magnetospheric mass density is in determining the frequencies of magnetospheric ultra-low frequency (ULF) waves, and hence the response time of the magnetosphere to perturbations. As well as varying with changes in the number density of the electrons and ions, the ion composition contributes significantly to the plasma mass density. Therefore, it is of scientific interest to understand the plasma ion composition and its spatial variations.

The plasma populating Earth's magnetosphere has two sources. Entry of the solar wind into the magnetosphere supplies light ions (H^+ and He^{++}), whereas plasma of ionospheric origin has a different composition. Observations show that although ionospheric plasma consists predominantly of H^+ ions, an enhanced supply of heavy ions, in particular O^+ , can occur [Shelley *et al.*, 1972, 1982; Lockwood *et al.*, 1985; Chappell *et al.*, 1987; Andre and Yau, 1997; Yau and Andre, 1997; Haaland *et al.*, 2013]. The heavy ion loading of the magnetosphere depends on a range of dynamical processes resulting in the transport of heavy ions to the closed inner magnetosphere, and at times, the presence of O^+ ions can represent a significant proportion of the magnetospheric plasma [Chappell, 1982; Young *et al.*, 1982; Horwitz *et al.*, 1984, 1986;

Roberts et al., 1987; *Comfort et al.*, 1988; *Andre and Yau*, 1997; *Yau and Andre*, 1997; *Moore et al.*, 1999; *Winglee*, 2000; *Korth et al.*, 2002; *Kistler et al.*, 2006; *Howarth and Yau*, 2008; *Haaland et al.*, 2009; *Liao et al.*, 2010; *Nosé et al.*, 2011; *Haaland et al.*, 2012a, b; *Li et al.*, 2012; *Slapak et al.*, 2012; *Nosé et al.*, 2015]. This study aims to use direct observations of ion composition to determine an empirical model of how the average ion mass is distributed in the closed magnetosphere, in a region covering the outer heavy ion torus, plasmatrough, and near-Earth plasma sheet, considering both variations in the equatorial plane and the distribution of average ion mass along magnetic field lines.

Multiple studies examining the ion composition in the closed magnetosphere exist, although they are not without limitations. Many studies examine ion composition using measurements of the O^+/H^+ density ratio, representing the concentration of heavy ions in the plasma [*Mouikis et al.*, 2010; *Ohtani et al.*, 2011; *Lee and Angelopoulos*, 2014; *Maggiolo and Kistler*, 2014]. *Mouikis et al.* [2010] examined the spatial distribution of the O^+/H^+ density ratio, using Cluster CODIF (ion Composition and Distribution Function analyser) measurements taken close to the equatorial plane. The data covered radial distances from 15 to 19 R_E , in the plasma sheet region. The analysis provided information on the MLT variations in the ion composition, however, the dependences were not quantified and variations with L shell were not considered. *Maggiolo and Kistler* [2014] also used Cluster CODIF data to produce statistical maps showing the O^+/H^+ density ratio in the equatorial plane. The measurements were constrained to plasma corresponding to an observed isotropic distribution, allowing mapping along the field lines, considering the near-Earth plasma sheet population within radial distances of 7 to 8 R_E , as well as in the midtail region (15 to 20 R_E). Other datasets have also been employed to examine the spatial distribution of the O^+/H^+ density ratio in the equatorial plane. *Ohtani et al.* [2011] presented

Geotail EPIC (Energetic Particle and Ion Composition) observations for the plasma sheet covering radial distances from 5 to 32 R_E , and *Lee and Angelopoulos* [2014] used THEMIS data over L shells from approximately 6 to 12. However, these studies are restricted to observations describing the equatorial distribution, and do not consider variations along magnetic field lines, which can provide some important information concerning the transport of heavy ions to the closed magnetosphere. A study conducted by *Denton et al.* [2009] used an indirect technique to observe the distribution of average ion mass along the field lines. Using measurements of multi-harmonic toroidal Alfvén wave frequencies, obtained by the Cluster spacecraft, the distribution of mass density, ρ , and electron density, n_e , were obtained, which provided a distribution of average ion mass (ρ/n_e) along the field lines. This technique was applied to only two case studies, as opposed to a statistical study. Furthermore, the inversion technique utilised to indirectly estimate the mass density makes several simplifying approximations, and requires functional forms for the dependences along the field lines to be assumed.

A survey of existing work indicates that there are no empirical models providing a description of the average ion mass spatial distribution. An advantage of considering average ion mass, as opposed to the O^+/H^+ density ratio, is that the contribution to determining the total plasma mass density can be clearly interpreted, and influences from other ion species are also included. Observations have shown that He^+ can also constitute a significant proportion of the magnetospheric population at times, affecting the ion composition [*Yamauchi et al.*, 2014a]. By using a large dataset, providing statistically significant results with good spatial coverage, this study presents an empirical model detailing the distribution of average ion mass along the field lines, including dependences with L shell and MLT.

2. Instrumentation and Data Reduction

Data is obtained from the four identical Cluster spacecraft (C1, C2, C3 and C4), which are arranged in a tetrahedral configuration. The polar orbits of the spacecraft cross many key regions of the magnetosphere (see *Escoubet et al.* [1997] for further details), and so provide the necessary data coverage required for this study. The dataset used, obtained from the CSA (Cluster Science Archive), covers the time interval of 2001 - 2005.

This study uses data from the CIS (Cluster Ion Spectrometry) experiment [*Rème et al.*, 1997]. This includes the CODIF instrument (ion Composition and Distribution Function analyser), which is a high sensitivity, mass resolving spectrometer measuring the full three dimensional distribution functions of the key ion species in the energy range 0.025 - 40 keV/charge. Integrals of the resulting distribution function, with a time resolution of one spacecraft spin (4 s), allow the ion density to be calculated for each of the ion species, specifically H^+ , O^+ and He^+ . Although the CODIF instrument also measures the distributions functions of He^{++} ions, these are omitted from the dataset, as He^{++} density data is over-estimated due to strong contamination by H^+ ions. Using the densities, n_i , with the atomic mass, m_i , of each ion, i , the average ion mass, m_{av} , can be estimated from

$$m_{av} = \frac{\sum_i (n_i m_i)}{\sum_i n_i} \quad (1)$$

The ground calculated moments of the CODIF HS (High Sensitivity) data, limited to the MAG modes, as appropriate for the outer plasmasphere and plasmatrough regions, provide the ion density measurements. From this dataset, the inferred average ion mass measurements are obtained over the required time interval, although it should be noted that data from the Cluster

106 spacecraft C2 and C3 are not used (the CIS instrument is non-operational on C2 and there are
 107 instrumental issues with the CODIF sensor on C3).

108 An important aspect concerning the CODIF dataset that should be considered is the back-
 109 ground contamination of the measurements due to penetrating energetic radiation belt particles.
 110 Although the effects of the background contamination are reduced due to the time-of-flight
 111 method of analysis used by CODIF, a visual inspection of the energy-time spectrograms indi-
 112 cates that the occurrence of data contamination is not negligible. Furthermore, the background
 113 contamination effect is mass dependent, such that it is stronger for the O⁺ ions [*Mouikis et al.*,
 114 2014]. This results in overestimated O⁺ densities, and therefore overestimated average ion mass
 115 values, for observations with significant background contamination. Further details on the ef-
 116 fect of the penetrating radiation belt particles on the CODIF measurements are described by
 117 *Ganushkina et al.* [2011], *Kronberg et al.* [2012], and *Mouikis et al.* [2014]. In order to identify
 118 where the CODIF data is significantly affected by the background contamination, a sample of
 119 representative passes through the radiation belt regions were assessed for signatures of contam-
 120 ination. This sample consisted of 38 passes in total, for a range of different seasons and orbit
 121 configurations. Figure 1 shows the frequency of contamination of the CODIF data in this sam-
 122 ple as a function of the spacecraft L value. It is clearly apparent that the contamination of data
 123 occurs more frequently at lower L values, where the spacecraft is more likely to encounter the
 124 radiation belts and the radiation belt particles are more energetic. Based on the inspection of the
 125 sample spacecraft passes, CODIF data obtained by the spacecraft at L values below 5.9 are not
 126 used in this study, due to the high occurrence of background contamination. Data obtained at
 127 $L \geq 5.9$ is less likely to be contaminated. For example, between $5.9 \leq L < 6.5$, on average 4%
 128 of the data in the sample is contaminated compared to an average of 64% for $4.5 \leq L < 5.9$.

Therefore, restricting the CODIF data used to observations at L values at 5.9 or above will reduce the background contamination to a negligible effect.

2.1. Comparison to RPA Observations

In order to examine how representative the average ion mass dataset is of the total plasma population in this region, the following analysis has been conducted. The CODIF instrument includes the RPA (Retarding Potential Analyser) device [Rème *et al.*, 1997]. When CODIF is operating in the RPA mode, ion densities in the energy range of 0.7 - 25 eV/charge (relative to the spacecraft potential) are provided. Therefore, densities measured using the RPA mode, and the corresponding calculated average ion mass, represent the cold population of plasma, which may be significant population in this region. Figure 2 shows the correlation of ion density, n_i , observations, and calculated average ion mass, m_{av0} , values, for data obtained in the MAG modes, corresponding to higher energy particles (0.025 - 40 keV/charge), and the RPA mode, corresponding to lower energy particles (0.7 - 25 eV/charge). In total, 2419 values for the MAG modes and 236 values for the RPA modes are obtained over the full time interval, where the values correspond to data binned for position for each orbit and averaged (refer to section 2.2 for details on the binning). The data is binned for L shell, using a binsize of 0.1, and the L shell of each bin is indicated by the colour of the point in Figure 2. Figure 2a, Figure 2b, and Figure 2c show the correlation of ion densities of the key ion species (H^+ , O^+ , and He^+ , respectively) for the MAG mode and RPA mode of the CODIF instrument. It can be seen that the majority of the points for all of these panels (a,b,c) lie below the $y = x$ line, indicating that the densities observed by the MAG mode are, in general, greater compared to the densities observed by the RPA mode. This feature is further demonstrated by Figure 2d, which shows the corresponding total ion densities (summed over all ion species) for the MAG and RPA modes. The total ion

density is observed to be increased for the MAG mode, representing the higher energy population, in comparison with the observed total ion density for the RPA mode, which measures the cold population. This indicates that, for the region considered here, the cold population, observed by the RPA mode of CODIF, is not the dominant population, and the hotter population, observed by the MAG mode constitutes a larger proportion of the total plasma. This is not unexpected as the population observed by the RPA mode, at these L shells located predominantly outside of the plasmasphere, are generally considered to correspond mainly to detached plumes and is not typically a major component of the plasma in this region [Dandouras *et al.*, 2005; Darrouzet *et al.*, 2009]. On the other hand, the MAG mode observations generally represent the ring current, plasma sheet, and other energised populations [Dandouras *et al.*, 2009; Yamauchi *et al.*, 2014b, a], a significant proportion of the plasma for the considered L shells. An analysis of case studies where the CODIF instrument on-board one spacecraft was operating in MAG mode while the CODIF instrument on-board another spacecraft was operating in RPA mode allowed a comparison of these two corresponding populations at approximately the same time. Although details are not shown here for all case studies, an example is now briefly highlighted to support the findings.

Figure 3 shows observations obtained by the CODIF instrument during a perigee pass through the dayside magnetosphere for the interval from 21:00 UT on 20 October 2002 to 02:00 UT on 21 October 2002. The CODIF instrument was operating in MAG mode for Cluster 1 (blue), observing ions in the energy range of 0.025 - 40 keV/charge. Conversely, the CODIF instrument on-board Cluster 4 (red) was operating in RPA mode, where ion density observations correspond to the energy range of 0.7 - 25 eV/charge. Figure 3a shows the total ion density, n_i , and Figure 3b shows the H^+ ion energy spectrogram, where both are observed by Cluster 1 in the MAG

mode. Figure 3c and Figure 3d show the corresponding ion density and H^+ energy spectrogram, respectively, observed by Cluster 4 operating in RPA mode. The data have been binned for L value, using a bin size of 0.2, considering data from the inbound and outbound parts of the orbit separately. The observations in each bin are averaged, and plotted as a function of L . A comparison of the energy spectrograms shown in Figure 3b and Figure 3d appear to indicate that the cold population observed by the RPA mode is a continuation of the hot population observed by the MAG mode, with no separate cold population observed. This suggests that the cold and hot populations are of the same source. The corresponding spectrograms for He^+ ions and O^+ ions (not shown here) demonstrate the same feature. In order to directly compare ion density values for the L range of interest for this study, the observations shown in Figure 3a and Figure 3c are shown in Figure 3e. Taking the inbound and outbound parts of the orbit together, the L profile is shown for an L range appropriate for the region considered by this study. As for Figure 3a and Figure 3c, the data have been binned for L value using a binsize of 0.2, and observations in each bin are averaged. It can be clearly seen that the ion densities corresponding to the MAG mode of the CODIF instrument (blue profile) are greater than the ion densities observed in the RPA mode (red profile), by a factor of $\sim 2 - 6$. For lower L values, outside of the range considered in Figure 3e, the low energy ion densities are observed to dominate, as expected. However, this case study provides evidence that in the L range considered in this statistical study ($5.9 \leq L < 9.5$), the hotter ion population, observed by the MAG mode, is dominant relative to the colder ion population.

Overall the total density observed by the MAG mode, with energies ranging between 0.025 - 40 keV/charge, is the major population for this region. Figure 2e demonstrates that the average ion mass values measured in the MAG mode can also be reasonably used to represent the cold

population measured in the RPA mode. Figure 2e shows the correlation of average ion mass values calculated from ion density observations in the MAG mode with corresponding values in the RPA mode. It is clear from Figure 2e that, across all L values shown, the points lie very close to the $y = x$ line. This indicates that the average ion mass values at lower energies, as measured by the RPA mode, are approximately equal to the average ion mass values measured in the MAG mode. Therefore, it appears that the ion composition of the plasma in the region examined is relatively uniform over the ion energies. This analysis has demonstrated that although CODIF is unable to observe some of the cold plasma population (due to spacecraft charging) and some of the hot plasma population (above the CODIF energy range), given the consistent values of average ion mass from the RPA mode energy range (0.7 - 25 eV/charge) and the MAG mode energy range (0.025 - 40 keV/charge), it is reasonable to consider that the average ion mass calculated from the MAG mode is generally representative of the total plasma population. It is important to recognise that there may be an additional cold plasma population in the plasma sheet at times, which cannot be observed due to spacecraft charging [Seki *et al.*, 2003]. Due to the instrumental limitations of the CODIF instrument, the possible existence of an additional cold plasma sheet population cannot be accounted for in this study.

2.2. Data Reduction

In order to examine the spatial variations in the average ion mass, the following technique is used. For each orbit, the data is binned by position into $0.5 \times 0.5 \times 0.5 R_E$ bins, in the GSM (Geocentric Solar Magnetospheric) coordinate system. The average value and average time of measurement for the observations in each bin of the orbit is determined, where the number of observations that are averaged in a bin typically ranges from between 10 and 100. From the

position of each bin, the corresponding MLT can also be found. Over all orbits, the total number of passes through each bin is typically of the order 100.

The next step taken is to determine the L value for each position bin within each orbit, where the L value is the radial distance of the bin's field line in the magnetic equatorial plane. This is done by tracing the field line corresponding to the bin's position and average measurement time, as predicted by the T96 magnetic field model [Tsyganenko, 1996], and defining the T96 magnetic equatorial position as the point of maximum radial distance along the field line. However, for cases where the angular difference between the field line midpoint position and the point of maximum radial distance exceeds 10° , then the field line midpoint of the field line is used instead. This technique accounts for the highly compressed dayside field lines, and it should be noted that the critical angular difference of 10° has been empirically chosen from an analysis of a variety of field line configurations. The T96 magnetic field model is parametrised by the solar wind dynamic pressure, IMF (Interplanetary Magnetic Field) B_y and B_z components, and the Dst index. The parameter values corresponding to the average measurement time of each bin was obtained from the NASA/Goddard Space Flight Center OMNI dataset through OMNIWeb, for the 1-min averaged solar wind parameters, and from the World Data Center for Geomagnetism (Kyoto) dataset, for hourly averaged Dst values.

The procedure of determining the L values for each position bin allows any points where the field line is traced as open by the T96 magnetic field model to be discarded, as this study is concerned only with the closed magnetosphere. However, there are inevitably some measurements on open field lines inaccurately modelled as closed field lines, which would contribute to some discrepancies in values taken near the magnetopause. In order to remove points corresponding to open field lines, a method adapted from Clausen *et al.* [2009] is employed, which

will now be detailed. The top panel in Figure 4 shows an ion energy spectrogram obtained from CIS measurements using the HIA (Hot Ion Analyser) instrument [Rème *et al.*, 1997], which illustrates the change in ion populations during a portion of the C1 spacecraft orbit. The spacecraft passes from the cusp region, through the OCB (Open-Closed Boundary), into the closed dayside magnetosphere, through perigee and then into the northern cusp region via the OCB again. It is apparent that open field lines near the OCB are characterised by relatively high ion fluxes at approximately 0.2 keV energies (see fourth panel for the DEF (Differential Energy Flux) profile at 0.2 keV), which can be used to distinguish between open and closed field lines near the boundary. However, high ion fluxes at this energy range are also observed near perigee, which correspond to closed field lines, so the DEF profile of ions at 10.0 keV (third panel) is used to differentiate between these situations. This is done by identifying where the DEF of ions at 10.0 keV and 0.2 keV (third and fourth panel respectively) exceed empirically defined critical values (dashed horizontal lines), which are indicated as red lines in the corresponding plots. From a comparison, points are defined as being on closed field lines if they have a DEF of ions at 0.2 keV below the critical value of $1 \times 10^7 \text{ keV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ keV}^{-1}$ or a DEF of ions at 10.0keV above $6 \times 10^6 \text{ keV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \text{ keV}^{-1}$, which is demonstrated in the second panel, where red (black) points correspond to open (closed) field line measurements. Therefore, using HIA/CIS ion energy flux measurements, it can be determined whether the spacecraft is situated on open or closed field lines, where DEF profiles at two energies are used to distinguish between flux peaks for open field lines and at perigee. This method is applied to all points in the datasets, discarding any points identified to be on open field lines, and the resulting datasets demonstrate a reduction in the fluctuation of values close to the OCB, as expected. It should be noted here that whilst Clausen *et al.* [2009] used data from the PEACE (Plasma Electron and

Current Experiment) instrument on-board the Cluster satellite, we opted to use data from the HIA/CIS instrument instead, as this provides better data coverage over the required interval.

The resulting average ion mass dataset, binned for position with corresponding MLT and L values determined, and all measurements corresponding to open field lines removed, is now examined. Variations with magnetic latitude and L value in the CODIF dataset can be examined from the average ion mass distribution in the X-Z plane of the SM (Solar Magnetic) coordinate system. The SM coordinate system is characterised by the geomagnetic dipole axis aligned with the Z axis, whereas the GSM coordinate system is defined such that the dipole axis is in the X-Z plane. Therefore, the SM coordinate system is more appropriate for assessing variations with magnetic latitude and L value, and is used in this case. A coordinate transformation is used to determine the position in the SM coordinate system corresponding to each bin's position in the GSM coordinate system, taking bins over each orbit individually. The distribution of average ion mass is shown in Figure 5a in the X-Z plane, with the colour of each point representing the average value of the measurements at that position (note that all measurements are now averaged over the number of orbit passes through the position bin). The measurement positions have been azimuthally mapped into the noon-midnight meridian, such that the radial distance from the Z axis is represented as the magnitude of the X position, and averaged separately over the dayside and nightside MLT sectors. All measurements in the southern hemisphere are also mapped to the corresponding position in the northern hemisphere, as it is assumed that the distribution along the geomagnetic field is symmetric about the magnetic equator. Note that spatial distributions of the data shown are binned with a binsize of $0.5 R_E$.

In order to give an indication of the statistical significance of this spatial distribution, Figure 5b shows the equivalent spatial distribution of the number of measurements averaged over MLT

in the X-Z SM plane. It can be seen that there are sufficient measurements in the dataset to provide a reliable spatial distribution over a significant range of L shells. It is noted that the orbital coverage over each year for this time interval is similar, and therefore, solar cycle effects are not a significant systematic bias in coverage along the magnetic field lines.

3. Average Ion Mass Distribution Along the Magnetic Field

Using the average ion mass dataset, the distribution along magnetic field lines can be examined, comparing data at different MLT and L values. This involves determining the most appropriate functional form to describe the distribution of average ion mass along the field lines. Then, using a least-squares fitting method to determine the best fitting function parameters, a hierarchical modelling approach [Clark and Gelfand, 2006; Tabachnick and Fidell, 2006] is employed to define a model function that includes the dependences on L shell and MLT. As the function parameters vary on multiple levels (dependencies on the L shell of the field line and the MLT are expected), the hierarchical method separately fits to each of these levels. Therefore the resulting best fit represents variations in the dataset as a whole, as opposed to variations confined to one level.

The average ion mass dataset, from measurements obtained by CODIF, provides sufficient spatial coverage along the field lines in the region spanning $5.9 \leq L < 9.5$. This corresponds to the outer heavy ion torus, plasmatrough, and near-Earth plasma sheet, which will be the region considered in the following analysis for the average ion mass distribution.

The average ion mass data are binned for the field line L value and the normalised radial distance along the field line, R_{norm} , which is the radial distance at which the measurement was obtained, R (R_E), divided by the L value of the field line. The T96 magnetic field model is used

here to determine the field line corresponding to each position bin, and the data are also binned for MLT (Magnetic Local Time) in order to further examine the spatial dependence.

An example plot showing the average ion mass as a function of normalised radius is shown in Figure 6 for an L shell of 7 (data are binned for L using a binsize of 1.). Logarithmic scales have been used in Figure 6, in order to linearise power law dependences. Each point represents the average value in the bin, where the normalised radius bin width is equal to 0.05, and the colour of the point corresponds to the number of averaged measurements in each bin, n . The vertical panels show the density data binned into 3 hour MLT intervals. The distribution of average ion mass values in each bin is indicated by the vertical grey line showing the range between the lower and upper quartile, with the short horizontal line representing the median value. As the profiles are smoothed using a boxcar function, with a width of 3 bins, some points are shifted relative to the grey lines. It can be seen from the example in Figure 6 that the average ion mass tends to maximise towards the magnetic equator and decreases off-equator, in agreement with results of previous studies [Takahashi *et al.*, 2004; Denton *et al.*, 2006].

To describe this dependence along the field line, a power law form is chosen, as shown in equation 2a:

$$m_{av} = m_{av0} R_{norm}^{-\beta} \quad (2a)$$

$$m_{av0} = 16.4 - 1.32L + (7.12 - 0.665L) \cos(15MLT + 32) \quad (2b)$$

$$\beta = -2.13 + 0.223L + (2.26 - 0.218L) \cos(15MLT + 219) \quad (2c)$$

where m_{av0} is the average ion mass at the magnetic equatorial point of the field line, and β is the power law index. The power law index, β , is required to be negative, which results in a

distribution where the average ion mass is a maximum at the magnetic equator and decreases towards the ionospheric ends of the magnetic field lines, as desired.

Using a least-squares fitting method, weighted by the number of measurements in each bin, the best fit parameters (m_{av0} and β) are determined for each field line distribution. Variations in the best fit parameters are then quantified to include dependences with L and MLT, providing a hierarchical model for a power law field line distribution. The resulting power law model (equation 2a, with model parameters given by equations 2b and 2c) is shown as the solid blue line in Figure 6. Although some MLT sectors do not appear to represent the best fit with minimum deviations from the data (e.g. second panel in Figure 6), this is due to the hierarchical technique employed. As mentioned previously, the model fits shown are results of fits at multiple levels, accounting for variations with L and MLT, as well as R_{norm} .

The functions used for all model parameters are chosen to include a sinusoidal term, so that the circular form describes the MLT dependence. The phase term of the sinusoidal component indicates the location of the peak of the parameter in degrees of MLT eastwards from the midnight meridian, and an amplitude term is included to determine the magnitude of the MLT dependence. Both the phase and amplitude terms are linear functions of L . An offset, which is also a linear function of L , is added to the sinusoidal term, to represent the mean value of the parameter across all MLT. The functional forms chosen to represent the MLT and L dependences have been chosen as they were the simplest forms that described the observed variations in the data, minimising the number of free parameters. Note that when fitting for the model parameters, if no clear L dependence in the data was observed, the L dependence was removed from the relevant functional form. The key features of the parameters, and the variations with L and MLT, are discussed in further detail in section 4.

Equation 2, representing the average ion mass distribution along magnetic field lines, is used to examine the azimuthally mapped spatial distribution in the X-Z SM plane. This is shown in Figure 7. In addition, the spatial distribution in the T96 magnetic equatorial plane, predicted by the average ion mass model, is also shown in Figure 8.

4. Discussion

The empirical model for the average ion mass distribution along the field lines, presented in section 3, includes dependences on both L and MLT. The features apparent in the model will now be discussed in further detail, providing information on the processes influencing the heavy ion loading of field lines in the outer heavy ion torus, plasmatrough, and near-Earth plasma sheet regions of the closed magnetosphere.

The resulting variations along the field lines for average ion mass, presented in section 3, models the distribution to be a maximum towards the magnetic equator, and decreasing off-equator. Although there are no models (to our knowledge) describing the distribution of average ion mass along the geomagnetic field in quantitative detail, previous studies of the plasma mass density distribution along magnetic field lines suggest that the average ion mass should be locally peaked at the magnetic equator [Takahashi *et al.*, 2004; Denton *et al.*, 2006, 2009], in agreement with our field line distribution. The preferential concentration of heavy ions at the magnetic equatorial plane is expected due to the centrifugal force acting more effectively on heavier ions [Denton *et al.*, 2006, 2009], assuming similar temperatures for the ion species, and was described by Lemaire and Gringauz [1998] in terms of an effective gravitational potential well at the magnetic equator.

A key source of heavy ions in the region covered by the dataset, determining the variations of the average ion mass distribution along the field line with L and MLT, is the plasma sheet

population. It is known that enhanced ionospheric outflows of heavy ions occur in the cusp and nightside auroral regions [Shelley *et al.*, 1972, 1982; Lockwood *et al.*, 1985; Chappell *et al.*, 1987; Chappell, 1988; Andre and Yau, 1997; Yau and Andre, 1997; Peterson *et al.*, 2008; Liao *et al.*, 2010]. This plasma, which has an increased relative concentration of heavy ions, is convected into the plasma sheet and then Earthwards, populating the closed magnetosphere [Chappell *et al.*, 1987; Chappell, 1988; Yau and Andre, 1997; Cully *et al.*, 2003; Dandouras *et al.*, 2005; Kistler *et al.*, 2010; Liao *et al.*, 2010; Mouikis *et al.*, 2010; Haaland *et al.*, 2012b; Haaland *et al.*, 2013; Kronberg *et al.*, 2012]. The plasma sheet particles enter the inner magnetosphere on the nightside region, acting to increase the average ion mass for nightside MLT sectors. Therefore, it is expected that the plasma sheet population contributes to the average ion mass distribution, and the convection of plasma sheet ions into the considered region acts to preferentially enhance the average ion mass in the nightside closed magnetosphere.

The distribution of average ion mass along the field lines is modelled using a power law form (equation 2a), with a negative power law index, β , to represent a maximum in average ion mass at the magnetic equatorial plane, as discussed in section 3. Figure 9a (showing m_{av0} as a function of MLT and L) illustrates the dependences of the empirically modelled equatorial average ion mass parameter, m_{av0} , as defined by equation 2b. The equatorial average ion mass parameter, m_{av0} , (equation 2b) combines a linear function in L with a sinusoidal component. Equation 2b shows that the mean value of m_{av0} , averaged over all MLT sectors, decreases linearly with L value. The decrease of the equatorial average ion mass with increased L values is illustrated by Figure 8 and Figure 9a. This feature of the average ion mass distribution is in agreement with previous observations [Mouikis *et al.*, 2010; Ohtani *et al.*, 2011; Maggiolo and Kistler, 2014], and is thought to result from the mass dispersion of outflowing ionospheric ions. The heavy

ions in the closed magnetosphere predominantly originate from ionospheric outflows at high latitudes. As the plasma is convected into the plasma sheet, mass dispersion occurs, such that low energy O^+ ions enter the closed magnetosphere at lower L values compared to lighter ions [Lockwood *et al.*, 1985; Chappell, 1988; Andre and Yau, 1997; Yau and Andre, 1997; Haaland *et al.*, 2009; Maggiolo and Kistler, 2014]. This results in an L gradient of O^+ concentration, such that the average ion mass increases towards lower L values. Therefore, the observed L shell dependence of m_{av0} (see Figure 9a) is a consequence of the plasma sheet properties.

Equation 2b includes a sinusoidal component for the model parameter m_{av0} , which describes variations of equatorial average ion mass with MLT. Figure 8 and Figure 9a clearly show that the MLT dependence is such that m_{av0} approaches a maximum at approximately 2200 MLT, so the equatorial average ion mass is higher in the evening sector compared to the morning sector. This feature can be attributed to plasma sheet convection into the inner magnetosphere. Plasma sheet particles convect into the considered region from the nightside, such that the corresponding average ion mass enhancement will be predominantly localised to nightside MLT sectors.

The function describing the model parameter m_{av0} (equation 2b) also includes an observed L shell dependence for the amplitude of the MLT variation. It can be seen from Figure 9a, that the amplitude of the MLT variation decreases with L value. As the MLT asymmetry arises as a consequence of heavy ions originating from the plasma sheet, the MLT dependence is expected to be most significant in the region of enhanced heavy ion concentration. This occurs towards the lower L values, as previously mentioned.

Equation 2c defines the power law index, β , which includes a linear function, describing the dependence of the power law index (averaged over all MLT sectors) on L , and a sinusoidal component representing the MLT variations. The dependences on L and MLT are illustrated in

Figure 9b. It can be seen that β linearly becomes less negative for increased L values, moving away from the average ion mass enhancement. More negative β values at lower L values indicate a steep decrease in average ion mass values away from the magnetic equatorial plane, which is expected to be due to the large enhancement in heavy ions at the magnetic equator due to the effects of the centrifugal force acting on the ions. An additional consideration for decreasing β values with increasing L value is the corresponding increase in the flux tube volume and length. Considering ionospheric ions with similar lifetimes, the increased flux tube volume and length means that fewer heavy ions will be concentrated at the magnetic equatorial plane, resulting in flatter distributions along the field line.

The sinusoidal MLT variation of the power law index, β , shown by equation 2c, indicates that the most negative values are located at approximately 2100 MLT, which is clearly shown in Figure 9b. This is due to a decreased up-welling of ionospheric O^+ ions on the nightside field lines, as a result of reduced photoionisation from solar radiation [Young *et al.*, 1982; Lennartsson, 1989; Stokholm *et al.*, 1989]. This causes the values to decrease more rapidly from the equatorial enhancement towards the ionospheric ends for nightside field lines, thus causing a steeper distribution along the field line, represented by a more negative power law index.

Furthermore, the plasma sheet contribution acts to increase the gradient along nightside field lines, relative to the dayside. As previously discussed, the average ion mass enhancement due to both this feature is greatest for nightside MLT sectors compared to the dayside (see Figure 8 and Figure 9a). The increase in the relative concentration of heavy ions in the equatorial region of flux tubes in the nightside region corresponds to an increased gradient in average ion mass along the field line. The result is a more negative power law index, β , value on nightside field lines than dayside field lines, where the average ion mass is reduced.

The discussion of the average ion mass distribution has mainly focused on the contribution of the plasma sheet population, which is convected into the closed magnetosphere. However, an additional source of heavy ions, which will influence the average ion mass of the plasma in this region, is the heavy ion torus. The heavy ion torus is a region of enhanced O^+ densities located just outside the plasmasphere, with no corresponding enhancement for the densities of light ions [Chappell, 1982; Horwitz *et al.*, 1984, 1986; Roberts *et al.*, 1987; Comfort *et al.*, 1988; Berube *et al.*, 2005; Darrouzet *et al.*, 2009; Nosé *et al.*, 2011, 2015]. The increased O^+ concentration will clearly correspond to an increase in the average ion mass of the plasma in the heavy ion torus. The expected L value position of the heavy ion torus typically ranges from $L \sim 4.5 - 6.5$ [Nosé *et al.*, 2011], with decreasing heavy ion enhancements, indicating the outer edge of the torus, observed at $L \sim 6 - 8$ [Lee and Angelopoulos, 2014]. It has been proposed that the heavy ion torus is the result of the interaction between the plasmasphere and the ring current [Horwitz *et al.*, 1986; Roberts *et al.*, 1987; Nosé *et al.*, 2011]. This interaction is expected to be most intense in the evening region, just beyond the duskside bulge region [Roberts *et al.*, 1987; Burch *et al.*, 2001]. As only the outer edge of the heavy ion torus coincides with the L range considered by this study, it is expected that the heavy ion torus contribution is minor in comparison with the plasma sheet contribution for this region. Nevertheless, the heavy ion torus acts to increase the average ion mass at lower L values in the dusk MLT sectors, further intensifying the average ion mass enhancement shown in Figure 8.

5. Conclusions and Further Work

This study has obtained an empirical model describing the distribution of average ion mass along closed geomagnetic field lines, including dependences with L shell and MLT. This involved using observations obtained by the CODIF instrument on-board Cluster, for a time inter-

val spanning approximately 2001 - 2005, between $5.9 \leq L < 9.5$. A key result obtained is the inclusion of the observed enhancement of heavy ions, located at low L values in the evening MLT sector, expected to originate from high-latitude ionospheric outflows, in the average ion mass model. The resulting model provides an important insight into the heavy ion loading processes occurring in this region, and their dependences on L and MLT. Notable differences between this model and previous empirical models are the size and coverage of the underlying datasets, and that variations along the field lines have been considered, as opposed to only considering equatorial variations.

This study is to be furthered by examining variations in the spatial distribution of average ion mass with different parameters and indices, quantifying solar wind and geomagnetic activity dependences [Young *et al.*, 1982; Kistler *et al.*, 2010; Mouikis *et al.*, 2010; Ohtani *et al.*, 2011; Kronberg *et al.*, 2012; Ozhogin *et al.*, 2012; Maggiolo and Kistler, 2014; Maes *et al.*, 2015]. This will provide information on the processes occurring with varying conditions, and how they influence the resulting average ion mass distribution in the closed magnetosphere.

An area of future work involves determining a corresponding empirical model describing the total electron density distribution along closed geomagnetic field lines. By combining the model with the empirical average ion mass model presented here, the total plasma mass density spatial distribution can be estimated for the region considered. This is a key motivation, as variations in the total plasma mass density provide information on the morphology and dynamics of the magnetosphere, and has significant implications for a variety of magnetospheric processes (e.g. propagation of wave modes implicated in radiation belt energisation and decay, and magnetic reconnection rates).

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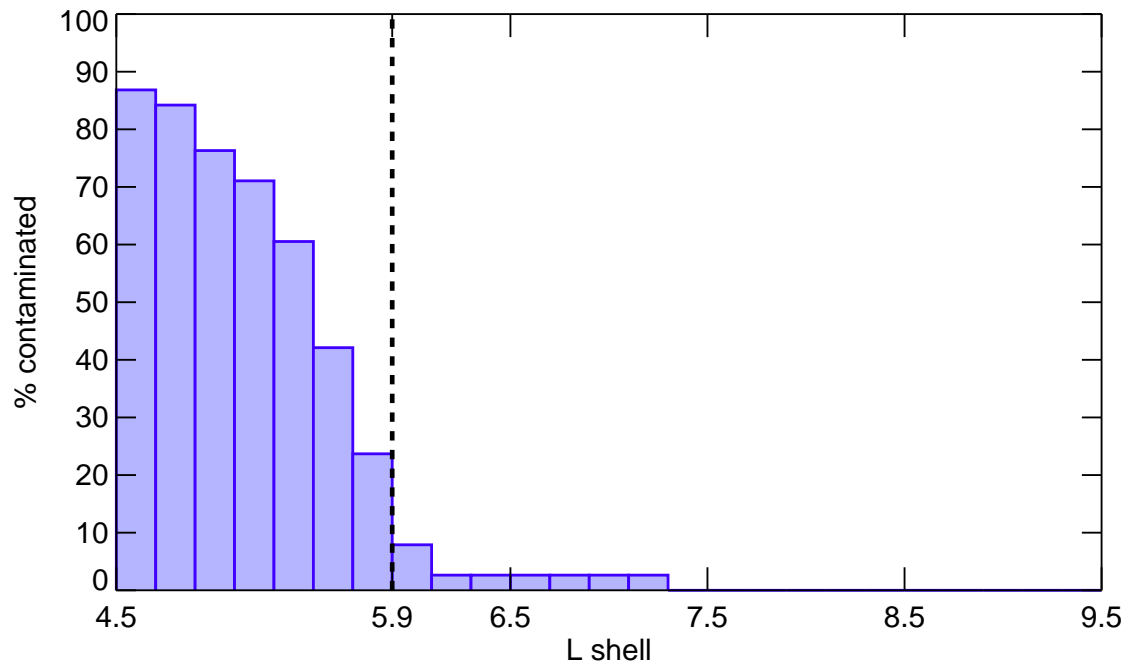


Figure 1. Histogram showing the percentage of cases where contaminated CODIF measurements, due to energetic radiation belt particles, were observed as a function of L shell. This is based on a representative sample of 38 passes through the radiation belt region. The vertical dashed line at $L = 5.9$ indicates the lower L shell boundary of CODIF data used in this study.

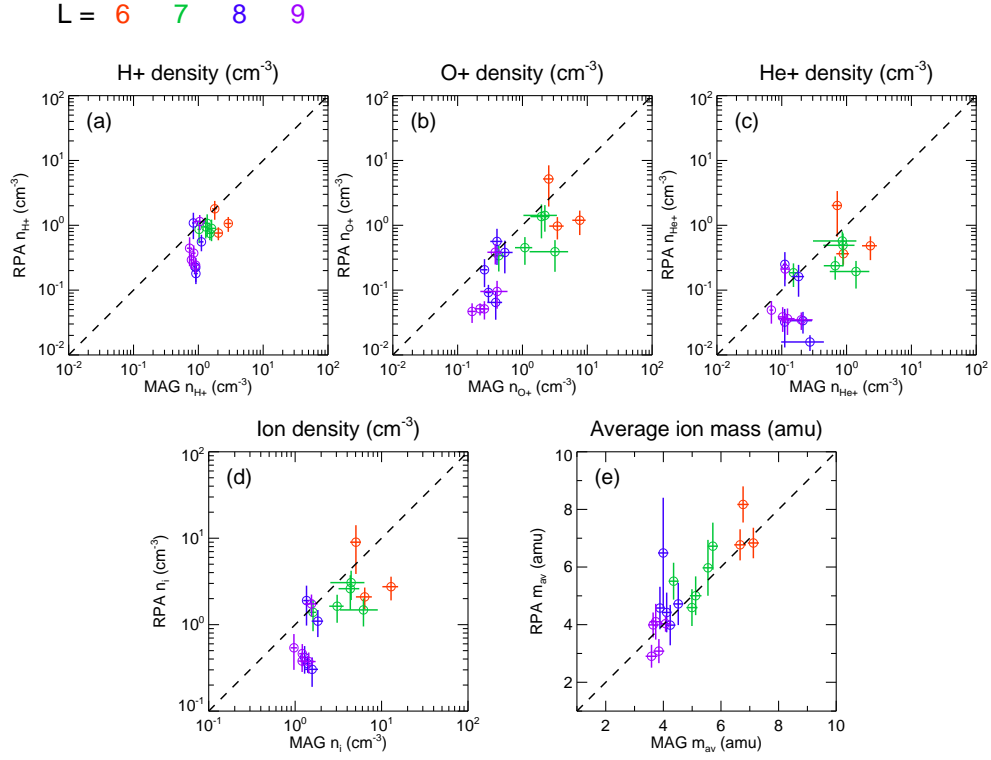


Figure 2. Plots showing correlations of CODIF measurements in the RPA (corresponding to 0.7 - 25 eV/charge energy range) and MAG (0.025 - 40 keV/charge energy range) modes. All data are binned for L value (represented by the colour of the points), with a binsize of 0.1, and the horizontal and vertical bars on each point correspond to the statistical standard error of the data in the L value bin. The dashed lines on each panel indicates $y = x$. Panels (a,b,c): correlation of H^+ , O^+ , and He^+ ion densities, n_{H^+} , n_{O^+} , and n_{He^+} , (cm^{-3}) respectively, measured by CODIF in the RPA and MAG modes. Panel (d): correlation of the total ion density, n_i , (cm^{-3}) measured by CODIF in the RPA and MAG modes. Panel (e): correlation of average ion mass, m_{av} , (amu) values calculated from CODIF measurements in the RPA and MAG modes.

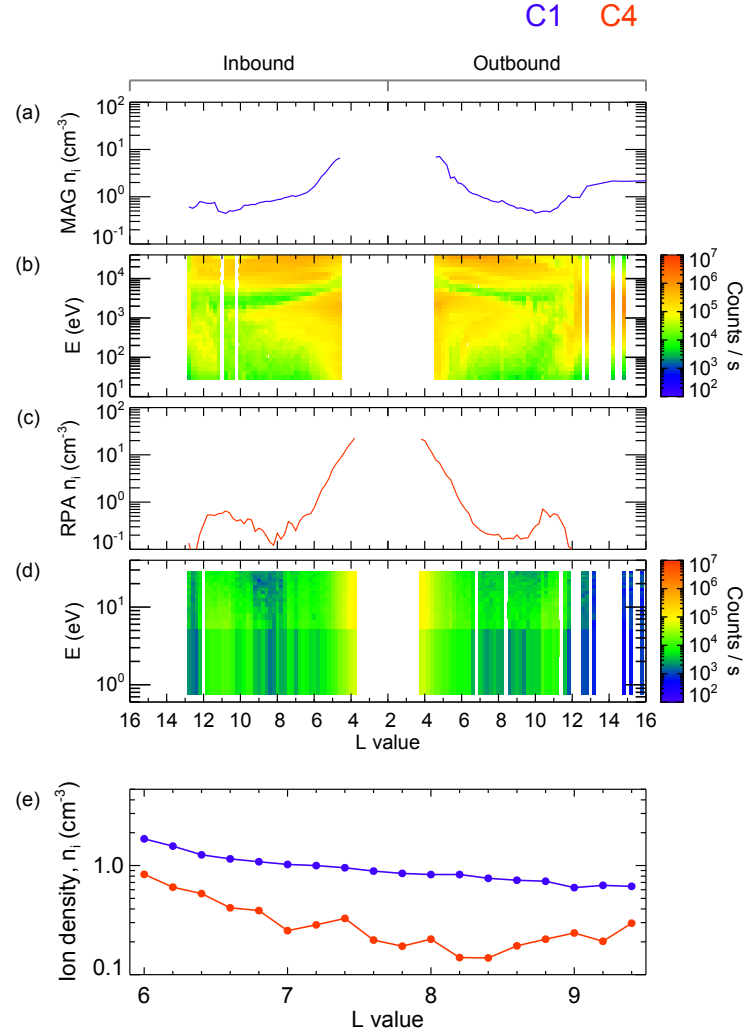


Figure 3. CODIF ion observations during a perigee pass for the interval from 21:00 UT on 20 October 2002 to 02:00 UT on 21 October 2002, for Cluster 1 (blue) and Cluster 4 (red). Panel (a) and panel (b) show the total ion density, n_i , and H^+ energy, E , spectrogram, respectively, observed by Cluster 1, where the CODIF instrument was operating in MAG mode. Panel (c) and panel (d) show the ion density and energy spectrogram, respectively, observed by Cluster 4, where the CODIF instrument was operating in RPA mode. Data in panels (a-d) are plotted as a function of L value, considering the inbound and outbound parts of the orbit separately, as labelled. Panel (e) shows the ion density variation with L , corresponding to the observations shown in panel (a) and panel (c) for $5.9 \leq L < 9.5$, taking the inbound and outbound parts of the orbit together.

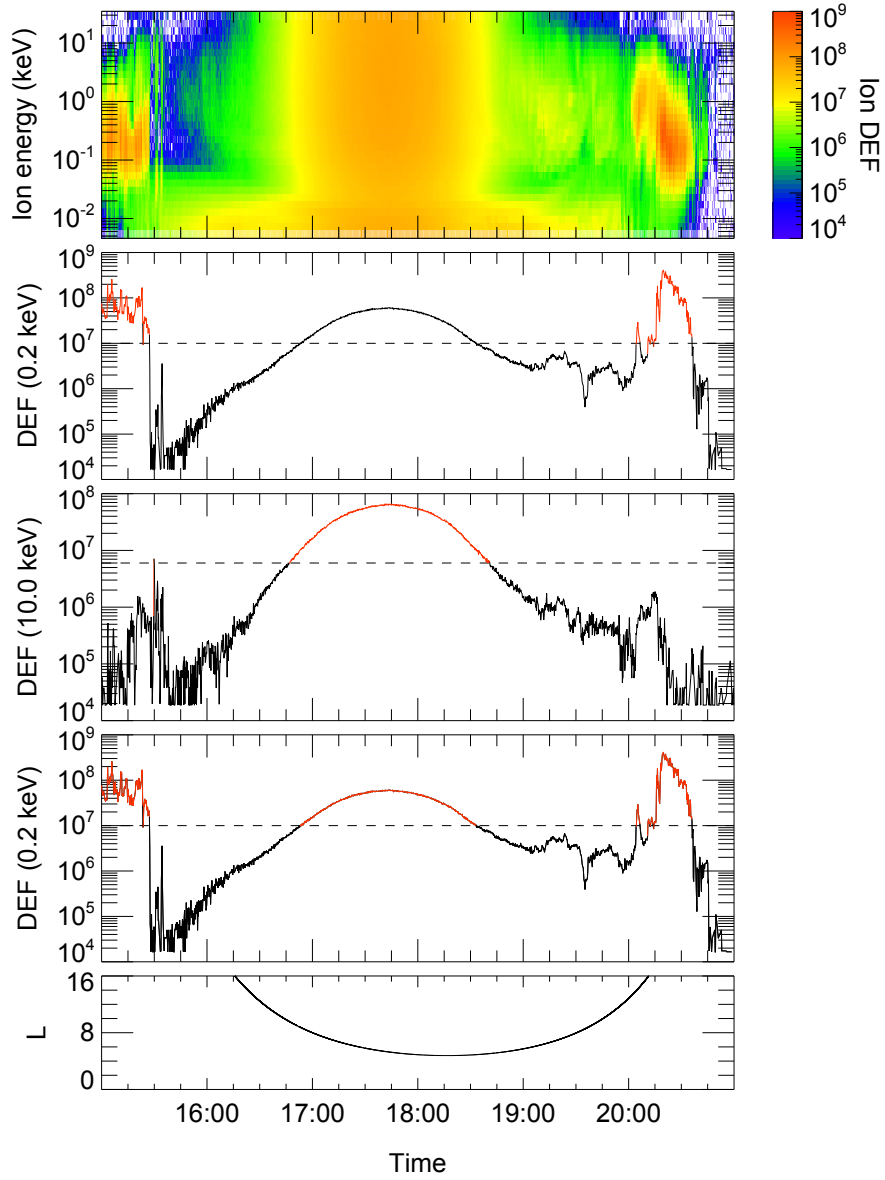


Figure 4. HIA/CIS ion energy flux data measured by C1 on 5 September 2002 (case study of *Clausen et al.*, 2009). First panel: ion energy flux spectrogram. Second panel: DEF (Differential Energy Flux) profile for 0.2 keV ion energies, with the red line corresponding to field lines close to the magnetopause that have been identified as open. Third and fourth panels: DEF profiles corresponding to ion energies of 10.0 keV and 0.2 keV, respectively, where the red line indicates where the values exceed a threshold (indicated by horizontal dashed lines). Fifth panel: L values of the spacecraft position.

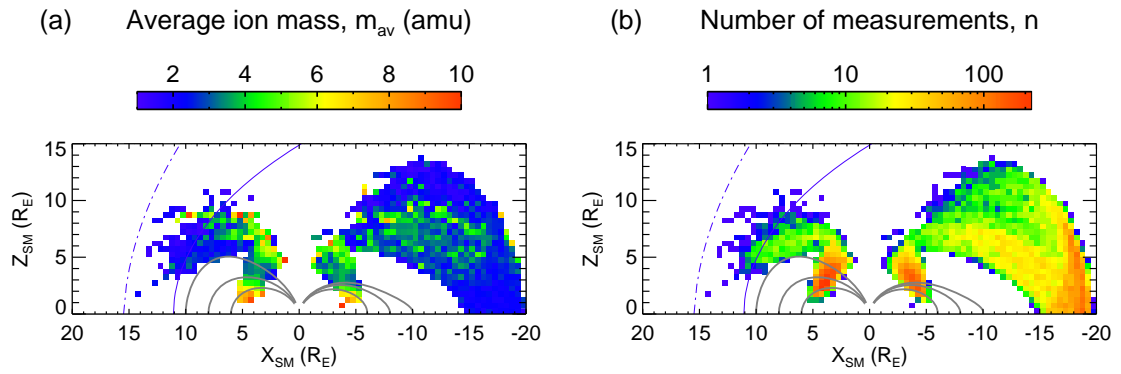


Figure 5. Spatial distribution of (a) average ion mass (amu) and (b) the number of measurements obtained by CODIF in the X-Z plane (SM coordinate system). The grey lines show reference T96 model magnetic field lines in the noon and midnight meridian planes, corresponding to spring equinox with a solar wind dynamic pressure of 2 nPa, for L values of 6, 8, and 10.

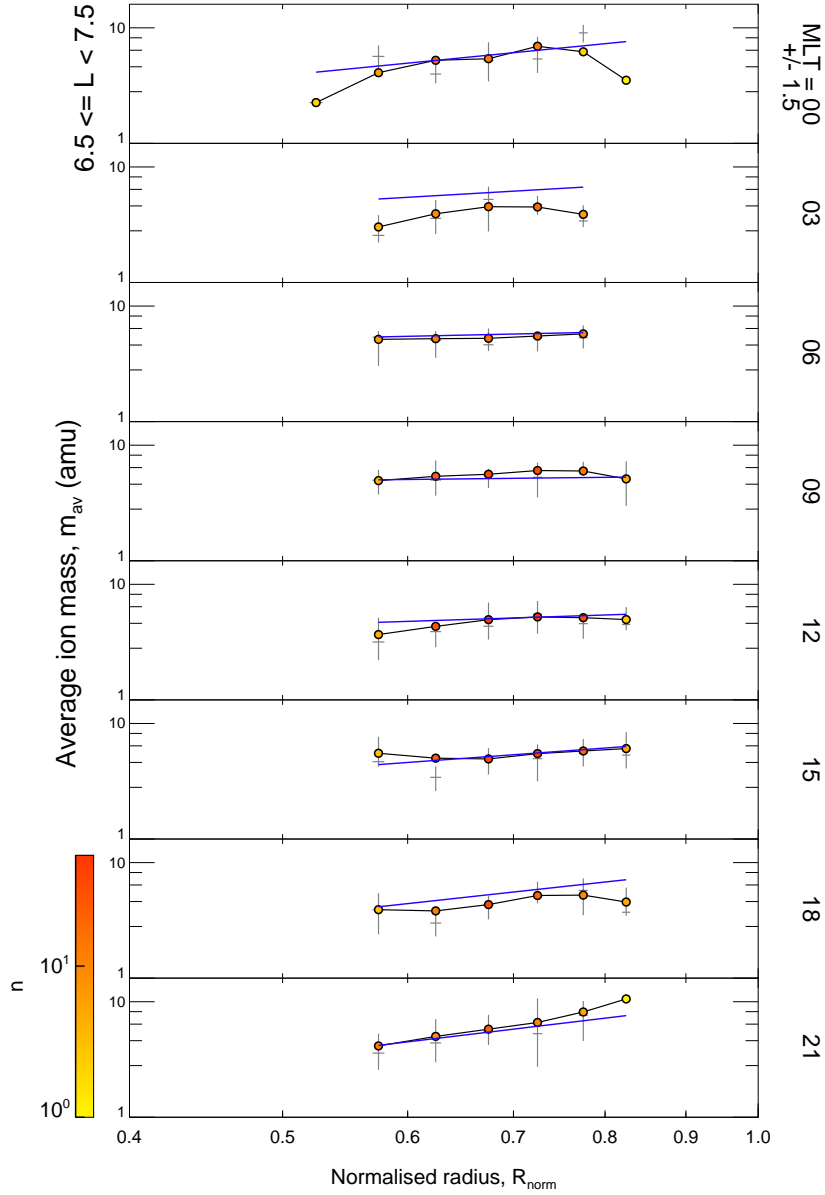


Figure 6. Average ion mass, m_{av} , (amu) plotted as a function of normalised radius, R_{norm} , for $6.5 \leq L < 7.5$ at 3 hour MLT intervals, where the colour of each point indicates the number of CODIF measurements, n , averaged in each bin. Note that a single CODIF measurement corresponds to an average of observations through a given position bin for one orbit. The upper and lower quartiles of the distribution of points averaged in each bin is shown by the grey line, intersected by a short horizontal line at the median value. The blue line represents the best fitting power law dependence.

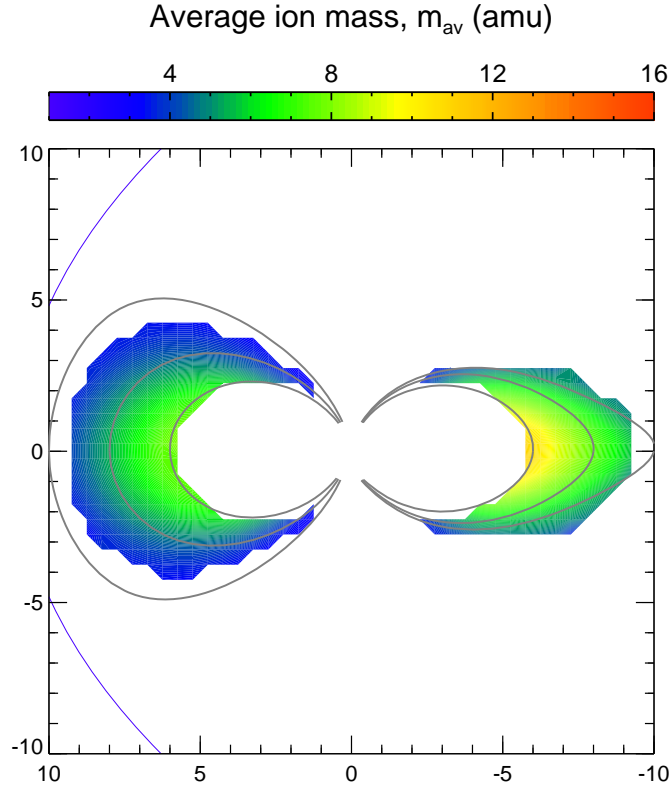


Figure 7. Spatial distribution in the X-Z SM plane using the average ion mass model. Note that the scales have been adjusted relative to the data plot (Figure 5) to focus on the most relevant regions. The grey lines show reference magnetic field lines in the noon and midnight meridian planes, for L values of 6, 8, and 10. The T96 magnetic field model used in this case corresponds to spring equinox, with a solar wind dynamic pressure of 2nPa.

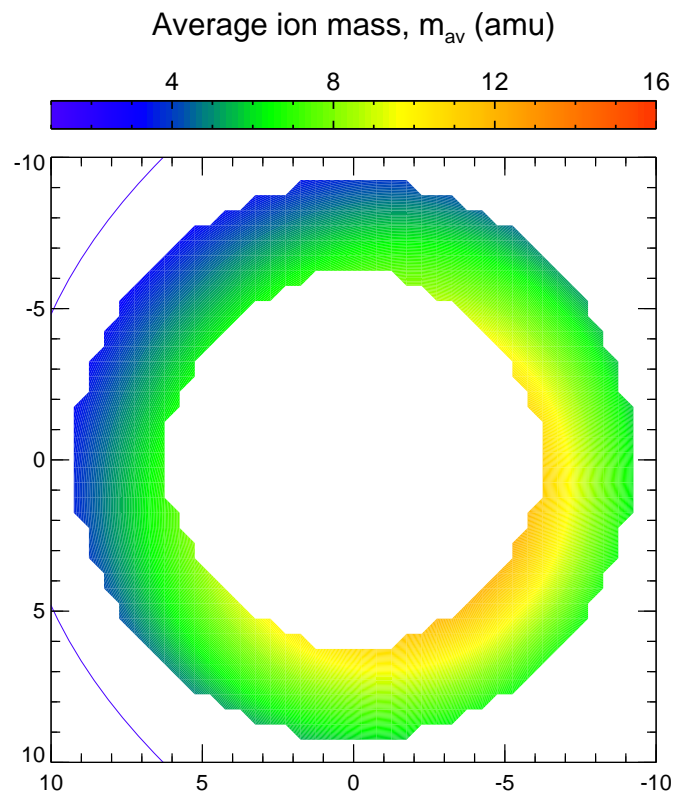


Figure 8. The spatial distribution of average ion mass in the T96 magnetic equatorial plane, in the same format as Figure 7.

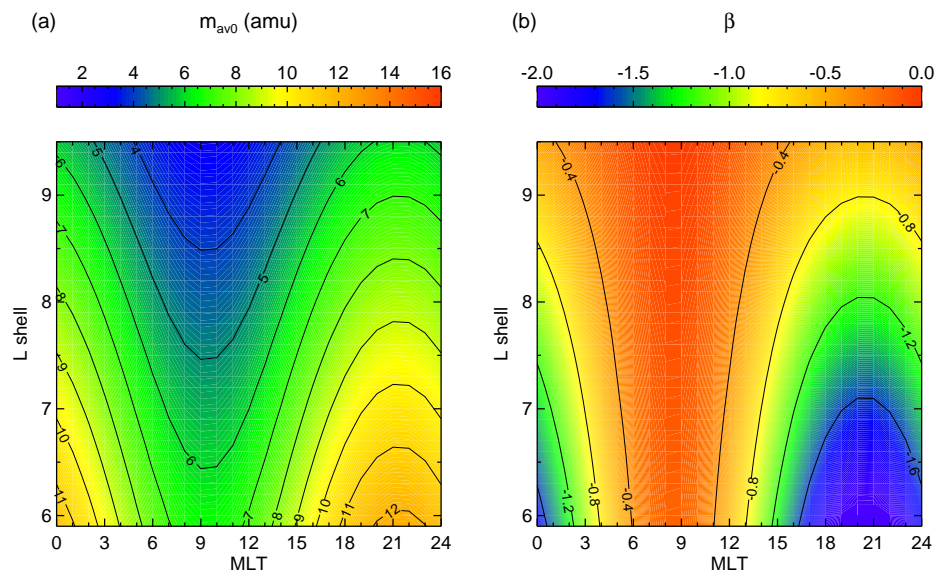


Figure 9. Contour plots showing the variation of the average ion mass model parameters (as defined in equation 2b and equation 2c) with L value and MLT.